



# Graded Exercise VLSI Design 2019:

## SAR ADC

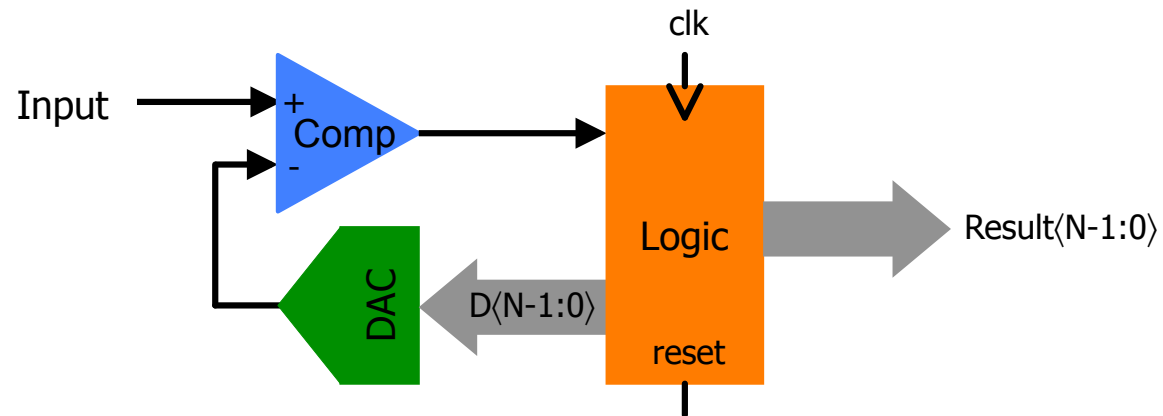
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# Successive Approximation ADC

- An Analogue – Digital – Converter (ADC) converts an analogue value (here a voltage) into a digital (here binary) code.
- An N bit ADC using the ‘successive approximation’ principle consists of
  - an N bit DAC (Digital – Analogue Converter) providing  $2^N$  (voltage) values from (in our case) 0 V to FSR (Full Scale Range)
  - an analogue comparator, comparing the input to the DAC output
  - a (clocked, digital) control logic which observes the comparator output and generates the DAC input word and the result





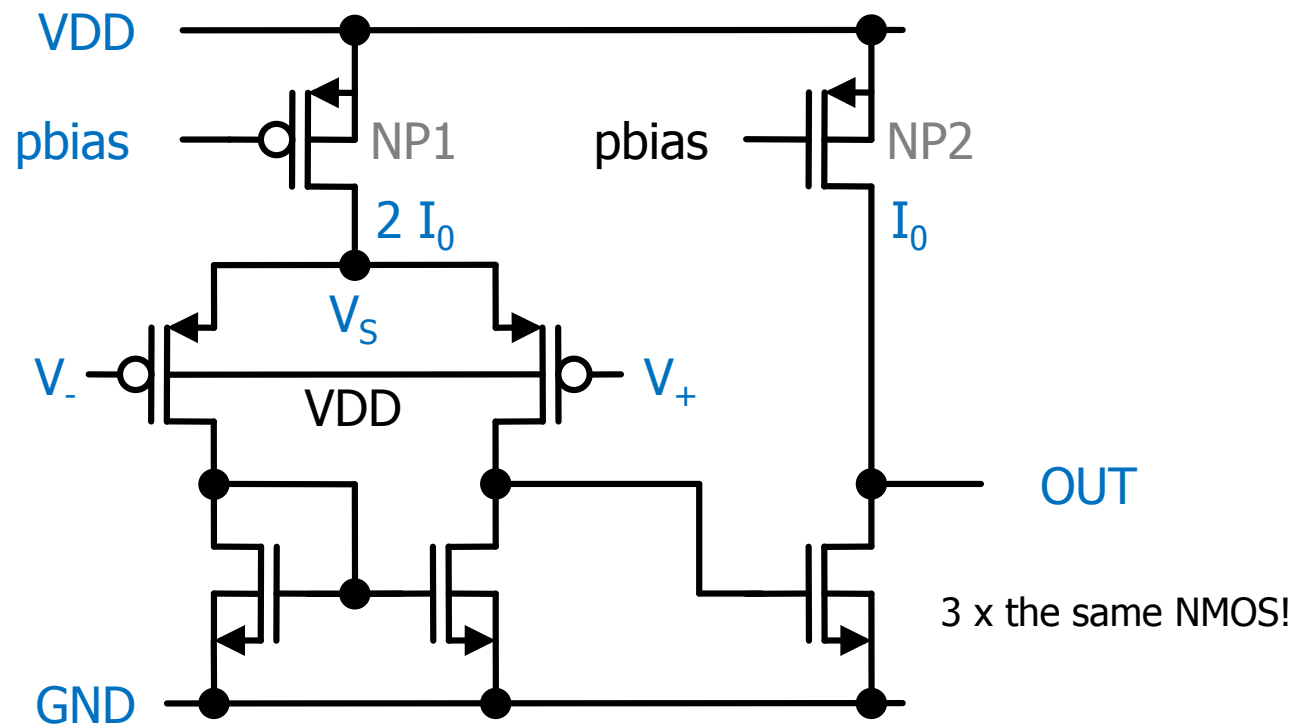
# Operation

- The SAR ADC operates in conversion cycles of  $N$  clocks
  - We assume that the input voltage is constant during the cycle (in practice, a Sample-and-Hold may be required at the input to 'freeze' a changing value)
- At the start of a cycle, the logic sets the DAC to  $\frac{1}{2}$  FSR
  - The comparator then finds out whether the input  $V_{in}$  is larger or smaller than this 'reference'
- At the next clock edge, the logic inspects the comparator output. This is the most significant bit (MSB) of the result.
  - If  $V_{in} < \text{FSR}/2$ , the logic sets DAC to  $\frac{1}{4}$  FSR
  - If  $V_{in} \geq \text{FSR}/2$ , the logic sets DAC to  $\frac{3}{4}$  FSR
- At the next clock edge, the next bit is extracted, and the DAC interval is again reduced by half, etc.
- With each clock, the difference between  $V_{in}$  and  $V_{DAC}$  is reduced to half and one output bit is generated



# The Comparator

- We use a very simple comparator with
  - a (PMOS) differential pair
  - followed by a (NMOS) gain stage





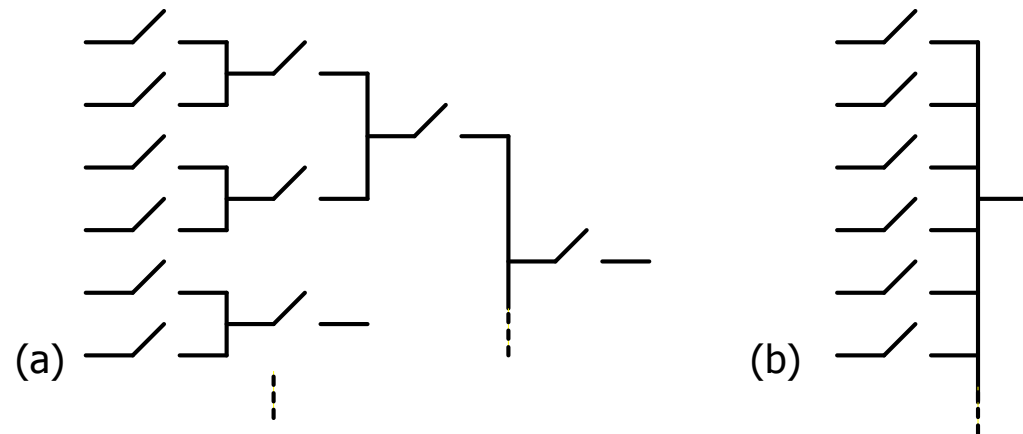
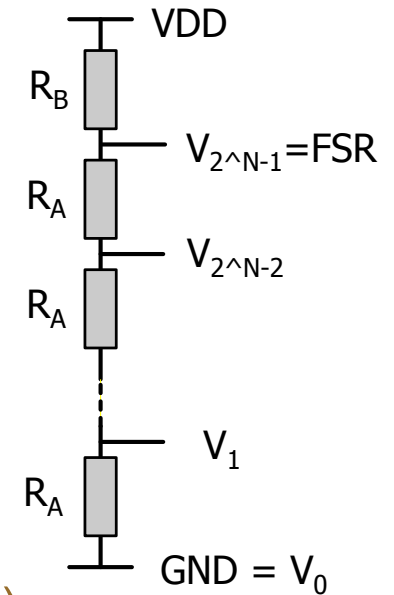
# The Comparator

- The comparator is biased with a ‘not too short’ PMOS current source NP1 ( $L \sim 1\mu\text{m}$ ).
  - Generate the bias voltage  $p_{\text{bias}}$  by a current mirror!
  - Use a current of – for instance –  $10\mu\text{A}$ .
  - For the sake of simplicity, generate the input current to the mirror with a resistor to ground.
- The second stage must be biased with *half the current* of the first stage so that its threshold is set to the condition  $V_+ = V_-$ . Try to understand why!
- This comparator can handle voltages at the inputs from (just) ground up to some positive voltage, but not up to  $V_{\text{DD}}$ .
- We will therefore restrict the voltage range FSR of our ADC (and thus of the DAC) to this maximal value



# The DAC

- We use a voltage divider made out of many equal resistors  $R_A$  with  $2^N$  taps to generate all possible voltages.
  - Because  $FSR < VDD$ , we have an additional resistor  $R_B$
- We then use analogue switches to implement a  $2^N \rightarrow 1$  MUX which selects one of the voltages, depending on the DAC input code.
  - The MUX may be implemented as a binary tree (a), or using one switch and a decoder per resistor (b)





# THE EXERCISE



# Goals for Grading

- In this exercise you should
  - Understand the SAR principle
  - Produce a well structured schematic hierarchy of the design
  - Provide analogue simulations of Comparator and DAC
  - Write a simple Verilog module for the control logic
  - Make a mixed mode simulation which shows correct conversion of a low, a medium and a high input voltage
  - Make 'nice', DRC and LVS error free layouts of Comparator and DAC
  
- These points should be documented in a short write-up with
  - a text describing your design decisions
  - text and screenshots of the simulation results, answering at least the question raised in the following
  - screenshots and explanations of your schematics layouts
  
- Use  $N = 5$  or  $6$ .





## Exercise 1: Understanding the SAR principle

- Write down the DAC output codes for the conversion sequences of some input voltages.
- Define an algorithm to generate the new DAC control word in the  $i$ -th step of the conversion.
- You may want to write a small program to check that your algorithm works



## Exercise 2: Simulating the Comparator

- Show that the comparator works:
  - Set one input to a fixed voltage  $V_1$  and sweep (DC or transient) the other input from a bit below  $V_1$  to a bit above  $V_1$ .
- Find out and understand for which voltage range of  $V_1$  the comparator works (at decent speed)
  - Try to extend the range as much as you can be sizing the transistors.
  - Make sure  $V_1 = \text{GND}$  is ok!
  - This fixes the FSR
- Check the speed:
  - The 'precision' of the comparator must only be  $\sim \text{FSR} / 2^N$ .
  - We can therefore define a figure of merit for 'speed' as the reaction time for a step input of this size around the threshold.
  - Does speed increase for higher bias current?
  - This speed sets your maximum clocking frequency!!!



## Exercise 2 cont.: Simulating the Comparator

- Input offset and common mode effects:
  - Does the comparator really switch *exactly* at  $V_- = V_+$  ?
  - Understand what happens!
  - Does this ‘input offset’ depend on the absolute input voltage level (The ‘common mode input voltage’) ?
- For our application, the input offset should be smaller than the LSB of our DAC...
  - What is the general effect of input offset on the transfer characteristic of the ADC ?



## Exercise 3. Simulating the DAC

- Chose the resistors such that the current in the DAC is not too high (compared to what?)
- Find arguments for the type of decoder to use and implement the schematic
- Simulate (best with a mixed mode simulation) that the decoder works as expected
- How long does it take to stabilize the output voltage for a large voltage step?
  - How does this depend on a load capacitance?
  - Which factors / components limit the speed? How?
  - Is the speed sufficient (compared to the comparator speed) when the capacitive load by the comparator is connected ?



## Exercise 4: The full ADC

- Write a Verilog module for the SAR algorithm and simulate the full ADC
  - Make sure the input voltage is stable during one conversion
- Simulate several input voltages in one simulation
  - You may stimulate the input with a piecewise linear voltage source pwl
- You may check that the ADC does *not* work any more if you run it too fast.
  - You could add an extra capacitance to the DAC output to artificially slow it down.



## Exercise 5: Layout

- Make the layout of the DAC such that
  - The resistance can be changed easily
  - The number of bits can be changed easily
- The layout of the DAC should be as compact as possible