

Solutions to Exercise: Intrinsic Carrier Density

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Constants

```
In[44]:= Nicm3 = 1.01 × 1010 (* carriers per cm3 *);  
         μe = 1400; μh = 480 (* cm2/Vs *);  
         q = 1.6 × 10-19 (* elementary charge in C *);
```

1. Carrier density in carriers per μm³

```
In[47]:= Niμm3 =  $\frac{\text{Nicm3}}{(10^4)^3}$  (* divide by 104 (cm → μm) for each space dimension *)
```

```
Out[47]= 0.0101
```

2. Current in a 200 × 200 μm² pixel at a bias of 100V

```
In[48]:= σ = q Nicm3 (μe + μh) (* Conductivity in As cm-3cm2/Vs = S/cm *)
```

```
Out[48]= 3.03808 × 10-6
```

```
In[49]:= ρ =  $\frac{1}{\sigma}$  104 (* Resistivity in Ω μm *)
```

```
Out[49]= 3.29155 × 109
```

```
In[50]:= R = ρ  $\frac{L}{A}$  /. {L → 300, A → 2002} (* everything is in μm, result is in Ohm *)
```

```
Out[50]= 2.46866 × 107
```

```
In[51]:= Curr =  $\frac{V}{R}$  /. V → 100 (* current result in in Ampere *)
```

```
Out[51]= 4.05077 × 10-6
```

3. Electrons / holes per nanosecond ?

```
In[52]:= Q = Curr 10-9 (* just multiply with 1 ns. Result is in Coulomb *)
```

```
Out[52]= 4.05077 × 10-15
```

```
In[53]:= Neh =  $\frac{Q}{q}$  (* Convert Charge to number of electrons per ns *)
```

```
Out[53]:= 25 317.3
```

Additional: Temperature Dependence of Carrier Density

```
In[54]:= Ni[TC_] =  $9.39 \times 10^{19} \left( \frac{TC + 273}{300} \right)^2 \text{Exp}\left[ -\frac{6884}{TC + 273} \right]$ 
```

```
(* Formula from Literature, temperature in Celsius *)
```

```
In[55]:= {Ni[17], Ni[27]} (* Compare 17°C and 27°C *)
```

```
Out[55]:= { $4.30494 \times 10^9$ ,  $1.01638 \times 10^{10}$ }
```

```
In[56]:= Show[(*Plot the temperature dependence,
also plot the same without the  $()^2$  term to show that it is small *)
```

```
LogPlot[ $\frac{Ni[TC]}{10^{10}} * \left\{ 1, \frac{1}{\left( \frac{TC+273}{300} \right)^2} \right\}$ , {TC, -40, 30},
```

```
PlotRange → Automatic, Frame → True, GridLines → Automatic,
PlotLabel → Style["Carrier Density /  $10^{10}$  vs. Temperature [C]",
14, FontFamily → "Arial"]]
```

```
, Graphics[{PointSize[Large], Red, Point[{27, Log[ $\frac{Ni[27]}{10^{10}}$ ]}]}]]
```

```
(* Show a point at 27°C *)
```

```
]
```

