



Exercise: Abstract Circuits

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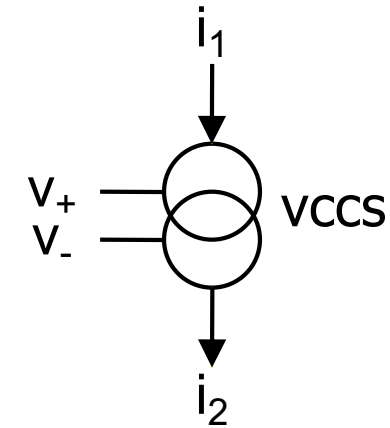
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Exercise 1: voltage controlled current source

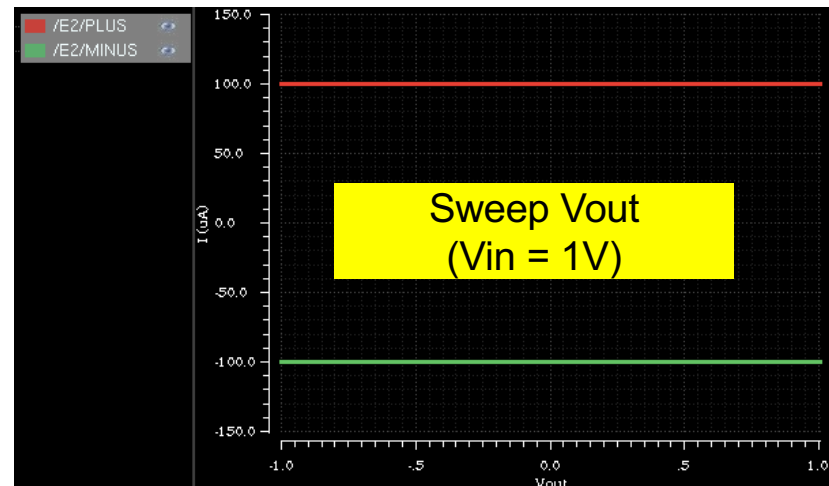
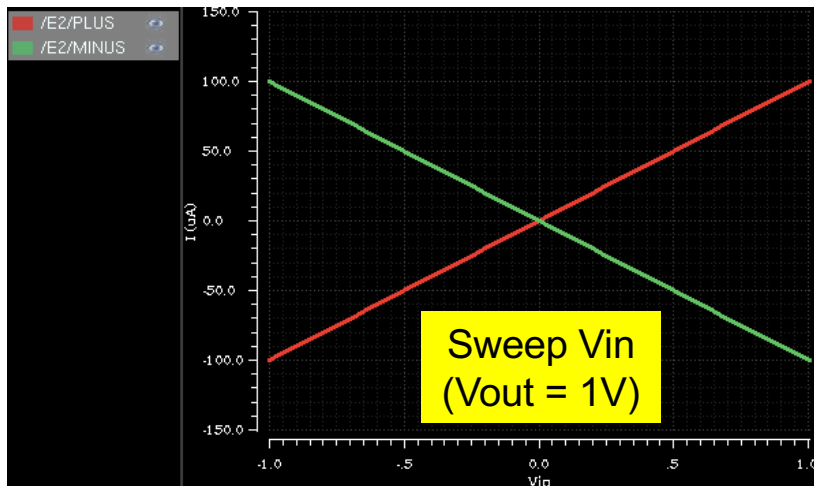
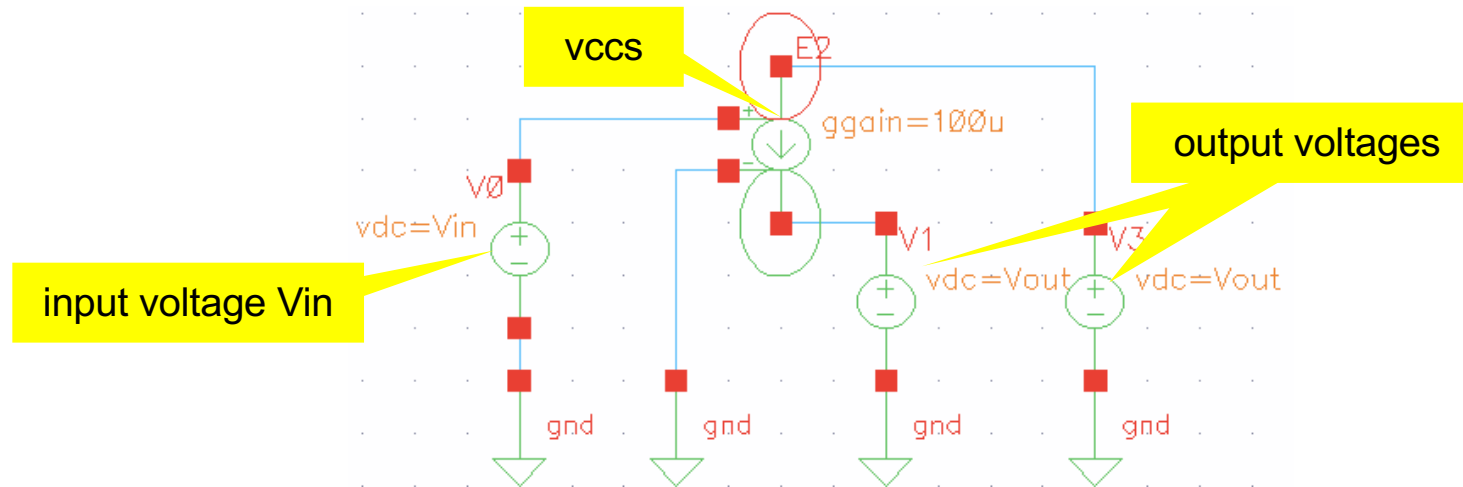
- The drain current in a transistor depends on the gate voltage. It can therefore be considered as a **voltage controlled current source** 'vccs'
- In the analogLib, the vccs has a differential input and two outputs of opposite signs:

$$i_1 = G (v_+ - v_-), i_2 = -i_1$$
- Set up the following circuit
 - Use a vccs with gain = 100 μ S
 - Connect v_- to ground and v_+ to a dc voltage V_{IN}
 - Connect the i_1 and i_2 outputs to $V_{OUT1} = 1V$ and $V_{OUT2} = 1V$
- Now
 - Sweep V_{IN} (DC sweep, for instance from -1V to 1V) and observe the currents in the output voltage sources. Change the gain of the vccs and observe the effect.
 - Does the output **current** for a given V_{IN} depend on the V_{OUT} ?





Solution 1



- The output current of these *ideal* sources does not depend on the output voltage



Exercise 2: Idealized Amplifier 1

- Implement the following circuit:

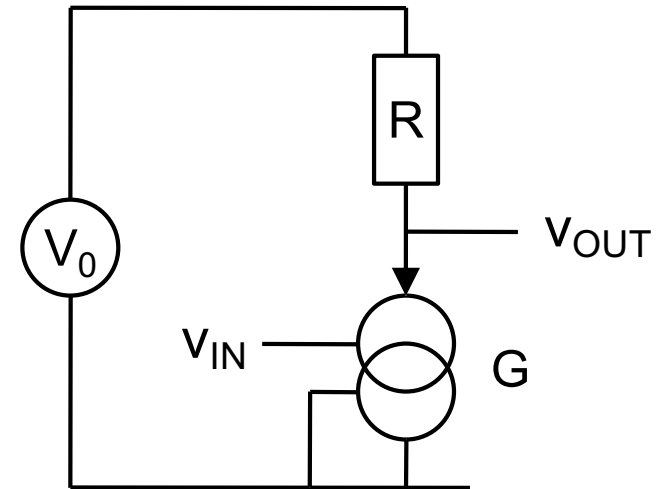
- The current from the v_{CCS} is sent to a resistor R

- Start with

- $G = 100 \mu\text{S}$
- $R = 2 \text{ k}\Omega$
- $V_0 = 1 \text{ V}$

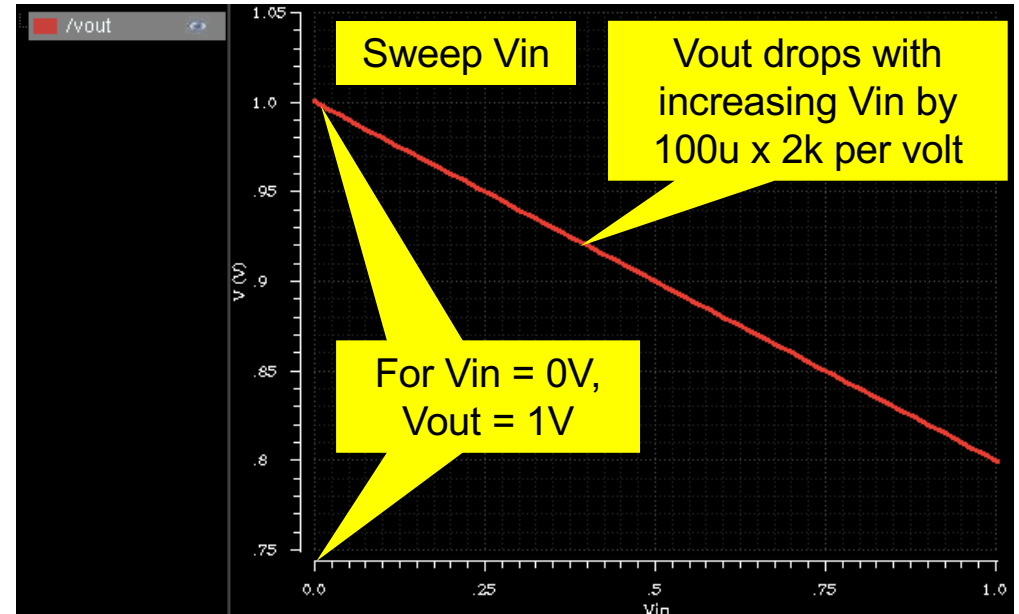
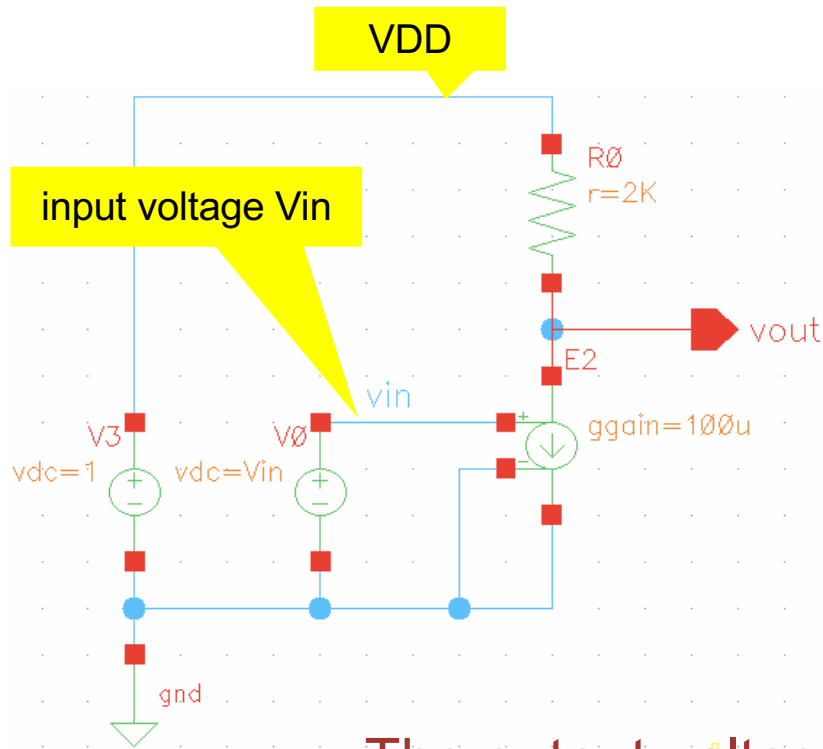
- Simulate:

- How does v_{OUT} change when v_{IN} changes (e.g. from 0 to 1 V) ?
- Explain (Calculate) ! Write down the current equation at node v_{out} and use $i_{VCCS} = G v_{in}$
- What is the gain of the circuit dV_{OUT} / dV_{IN} ?
- Change R and G in your simulation. Is the effect as expected (as calculated)?

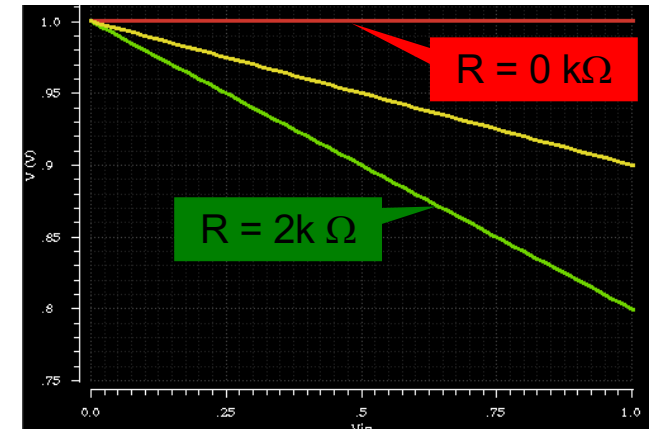




Solution 2



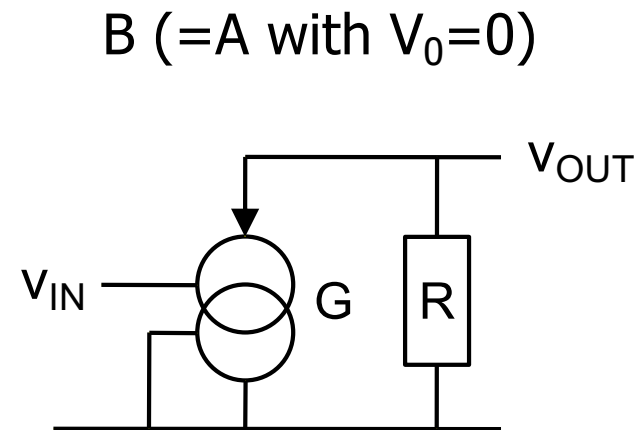
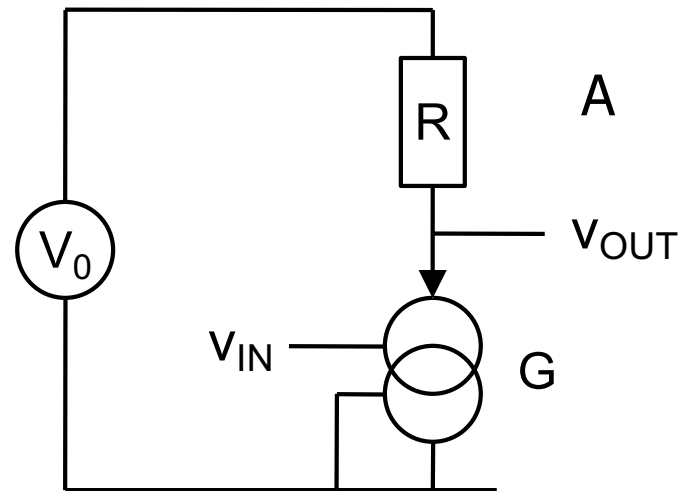
- The output voltage is $V_{out} = VDD - R \times I = VDD - R G V_{in}$
- The gain (slope) is $v = dV_{out} / dV_{in} = - R G$
- Changing R (0, 1kΩ, 2kΩ):



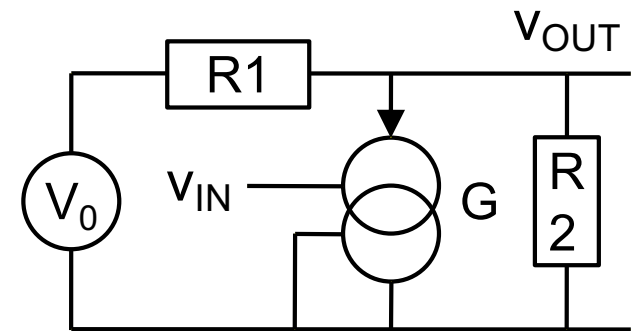


Exercise 3: Idealized Amplifier 2

- In the previous circuit, change V_0 . What happens with the *DC offset* of the output and with the *gain*? Explain!
- So, what is the difference between the following two circuits A,B ?



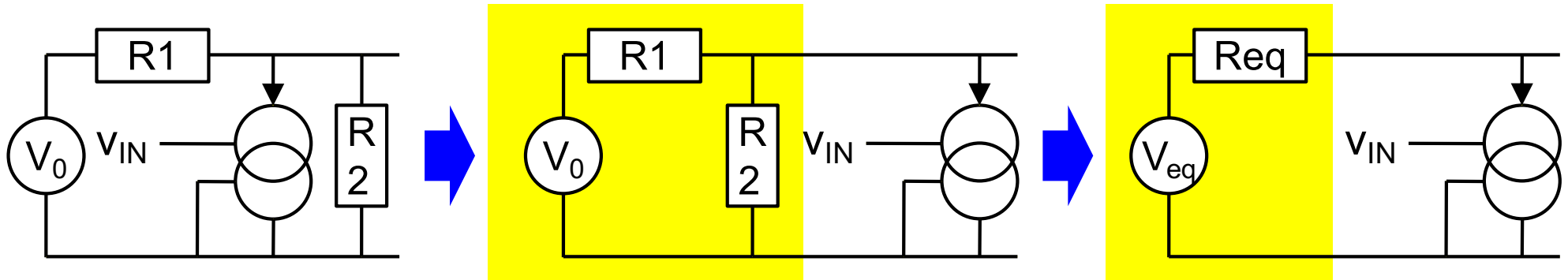
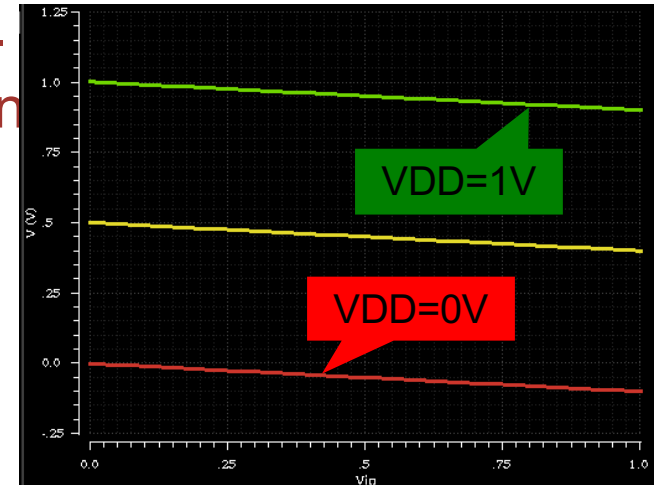
- **PREDICT** the gain ($V_{IN} \rightarrow V_{OUT}$) of the following circuit (Thévenin!):
- Verify this by simulation (for instance $R1 = 1 \text{ k}\Omega$, $R2 = 2 \text{ k}\Omega$)
- What happens when you exchange $R1$ and $R2$?





Solution 3

- Changing VDD just changes the offset (i.e. shifts the curve up and down)
 - With the ideal source, the circuit also works at VDD=0V.
- The gain of the two circuit is the same. For a gain analysis, we can drop VDD for simplicity!

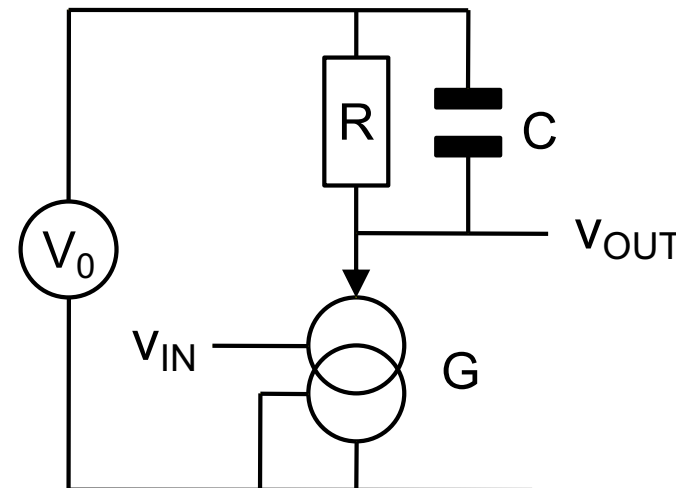
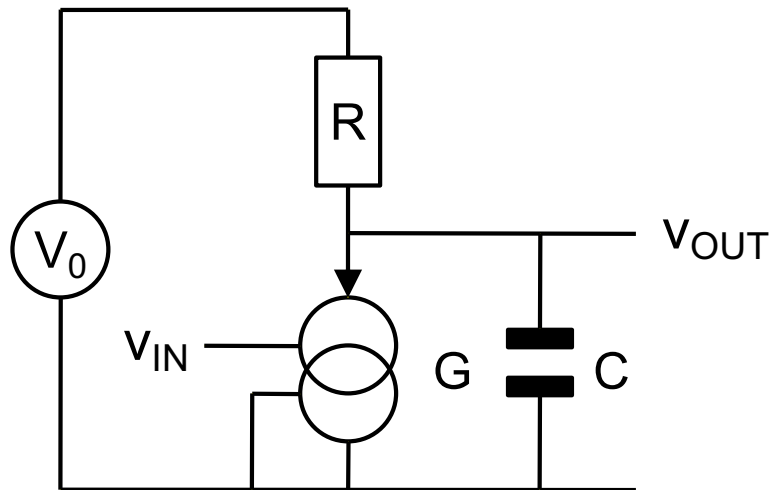


- $V_0/R_1/R_2$ can be replaced by V_{eq}/R_{eq} . R_{eq} is $R_1 \parallel R_2$. V_{eq} is irrelevant for gain. Gain becomes $G R_{eq}$.
- Gain is $-100\mu A \times 2k\Omega / 3 = -0.066$.
- Swapping R_1/R_2 makes no difference!



Exercise 4: Idealized Amplifier 3

- Load the output with a capacitor (1 pF) to ground (left) and make an *ac* sweep. What is the dc gain?
- Where is the corner frequency? Why?

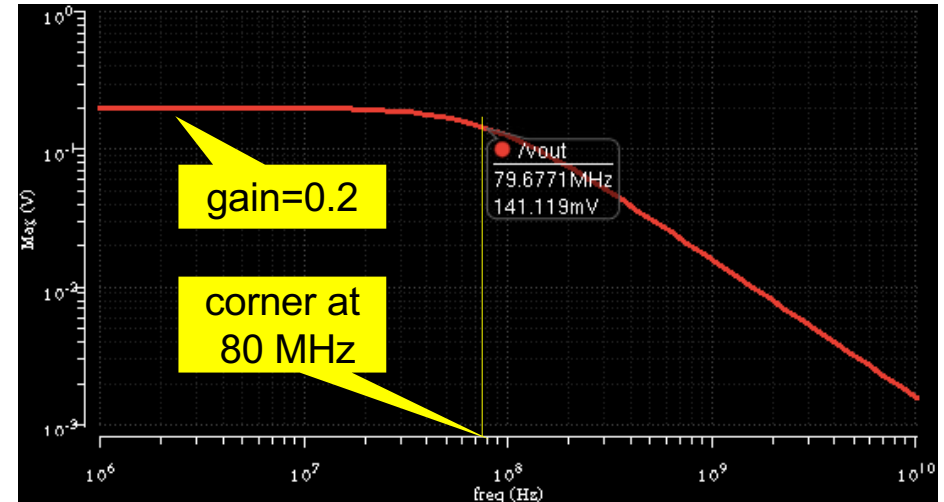
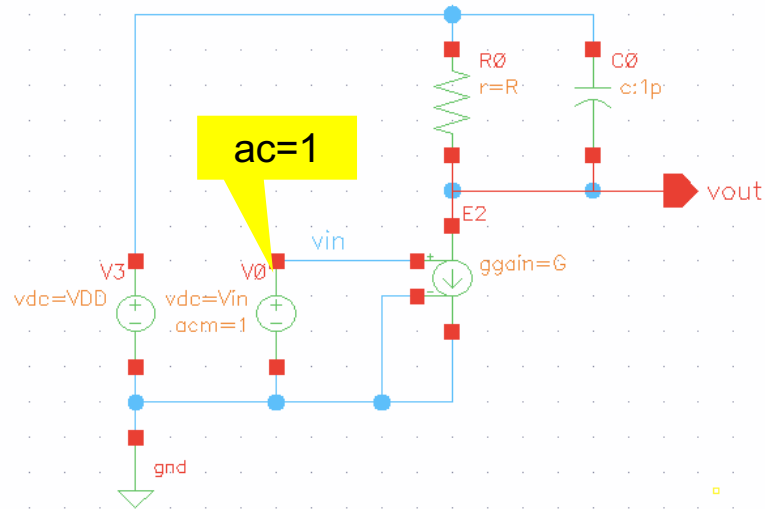


- Now try the right circuit. Is there a difference? Explain!
- Draw an equivalent circuit without V_0 !



Solution 4

- Remember to add an ac component to V_{in} !

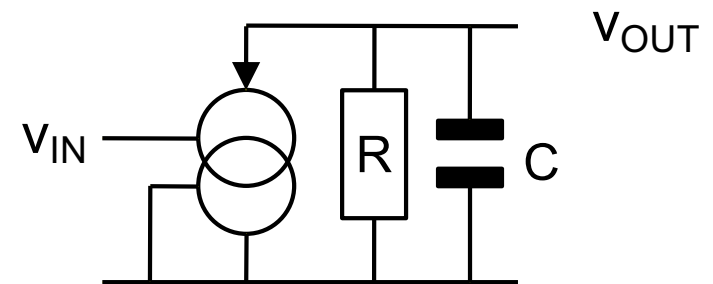


- We see a Low Pass behavior
 - DC gain is $100\mu \times 2k = 0.2$
 - Corner is at $\omega = 1/RC = 1/2n = 500M \rightarrow \nu = 500M/6.28 = 79.6 \text{ MHz}$

- Derivation by current sum at v_{out} :

$$G v_{in} + v_{out}/R + v_{out} s C = 0$$

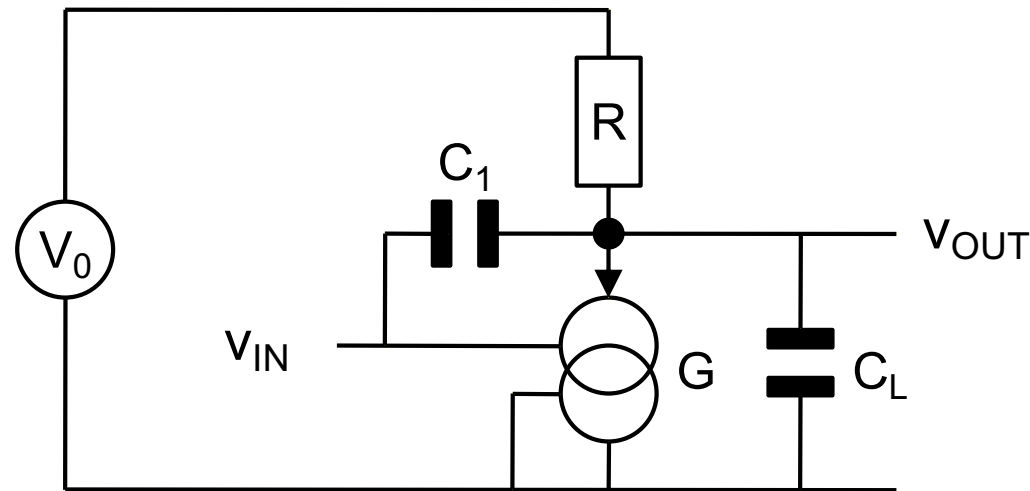
$$\rightarrow v_{out} / v_{in} = - \frac{G R}{1 + C R s}$$





Exercise 5 (advanced!): More capacitors

- Consider this circuit with an extra C_1 between V_{IN} and V_{OUT}



- Draw the circuit without V_0 !
- What gain do you expect at *dc* ? Sign?
- What gain do you expect for *very* high frequencies? Sign?
- Calculate the transfer function $H[s]$ and the gain
 - Verify your predictions
- Simulate the circuit



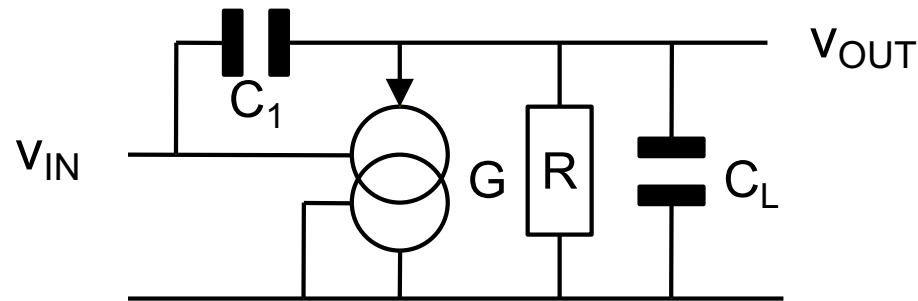
Exercise 5 cont. (For fun)

- Where is the pole, where is the zero?
- Chose the resistor value such that the pole and the zero are at the same frequency.
 - Does that always work?
 - What is the DC gain?
 - How does the transfer function look like?
 - What is the gain of the circuit vs. frequency?

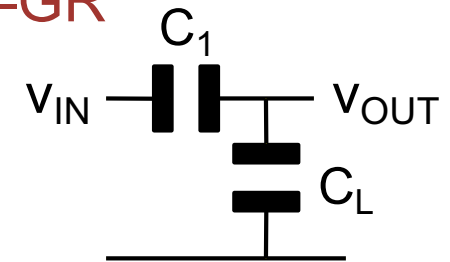


Solution 5

- All elements to VDD to to ground:



- Gain at DC (no caps) should be as before $-GR$
- At high frequencies, impedances of C dominate. We have a capacitive divider with gain $+ C_1/(C_1+C_L)$ (positive!)
- Derivation (current sum at v_{out}):



$$\text{Solve} \left[(v_{out} - v_{in}) s C_1 + G v_{in} + \frac{v_{out}}{R} + v_{out} s C_L = 0, v_{out} \right]$$

$$v = -GR \frac{1 - \frac{C_1}{G} s}{1 + R (C_L + C_1) s}$$

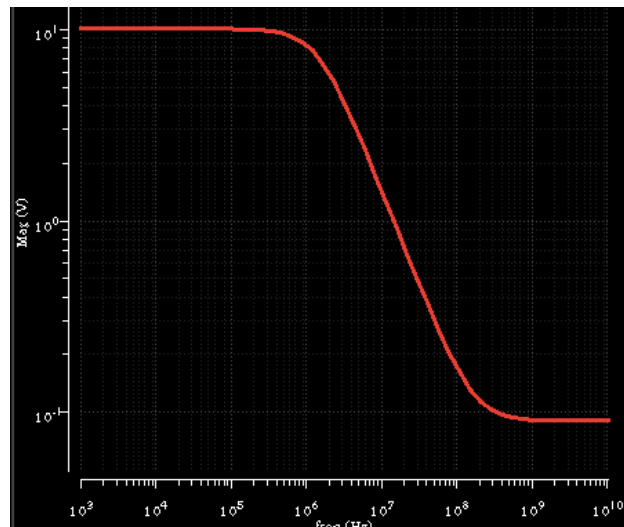
$$v \Big|_{s \rightarrow 0} = -GR \quad \text{Limit}[v, s \rightarrow \infty] = \frac{C_1}{C_1 + C_L}$$



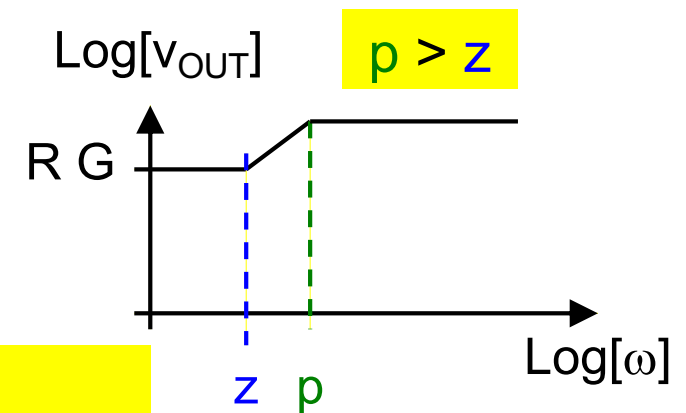
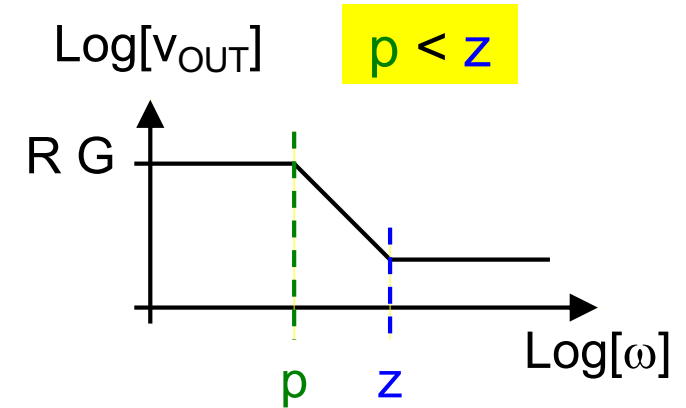
Solution5

$$v = -R G \frac{1 - C_1 / G s}{1 + R (C_L + C_1) s}$$

- We have a pole at $p=1/R(C_1+C_L)$ and a ZERO at $z=G/C_1$
- Gain changes from negative to positive!
- Bode Plot depends on whether pole or zero is higher frequency



Example for $p > z$:
 $G=100\mu$, $R=100k$, $C_1=0.1p$, $C_L=1p$
 $p = 1/R(C_1+C_L) \sim 1/RC_L = 10MHz$
 $z = G/C_1 = 1GHz$





Solution 5

- Setting pole and zero equal is always (i.e. for all values of $C1, CL, G$) possible:

In[48]:= `Solve[z == p, R]`

$$\text{Out[48]= } \left\{ \left\{ R \rightarrow \frac{C1}{(C1 + CL) G} \right\} \right\}$$

- (Note: This is not the case for, e.g., CL , which may have to be negative..)

In[40]:= `Solve[z == p, CL] // Simplify`

$$\text{Out[40]= } \left\{ \left\{ CL \rightarrow C1 \left(-1 + \frac{1}{G R} \right) \right\} \right\}$$

- The DC gain is $-C1/(C1+CL)$:

In[49]:= `v /. R -> Requal /. s -> 0 // Simplify`

$$\text{Out[49]= } -\frac{C1}{C1 + CL}$$

- The transfer function is just

$$-\frac{C1}{C1 + CL} \frac{G - C1 s}{G + C1 s}$$



Solution 5

- The s-part of this function has the form $(1-ks)/(1+ks)$.
- With $s = i \omega$, the absolute value is calculated by multiplying with the complex conjugate, i.e.

$$\frac{1 - k i \omega}{1 + k i \omega} \frac{1 + k i \omega}{1 - k i \omega}$$

which is 1.

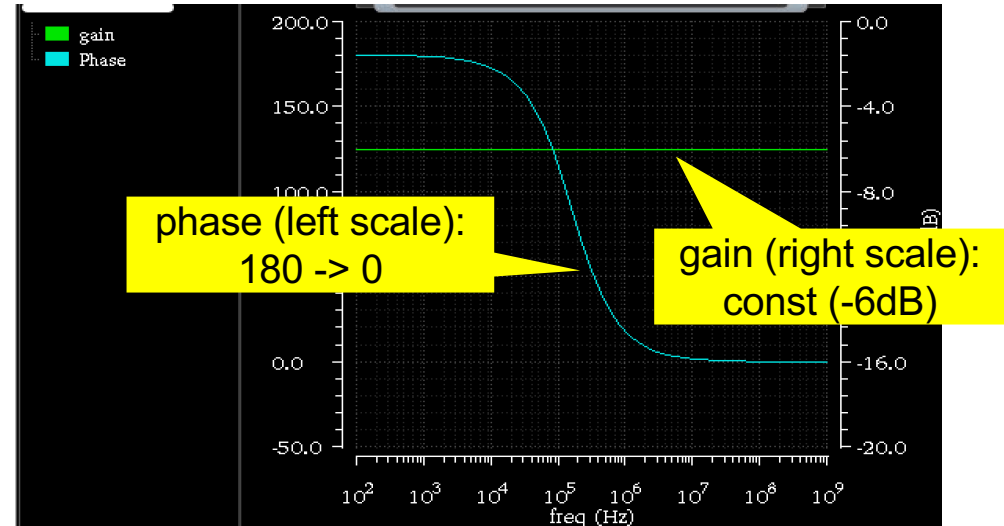
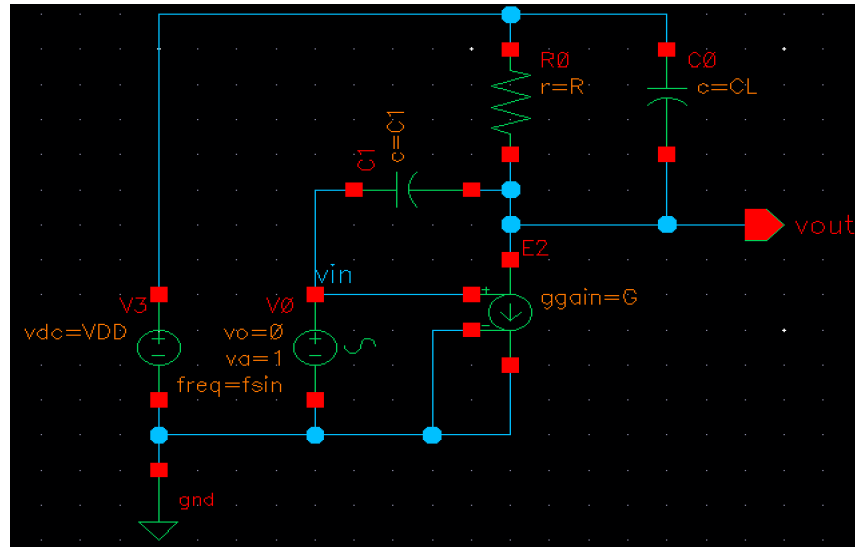
Therefore, the (absolute value) of the gain is constant!

- But the phase changes from inverting (180°) to non-inverting (0°). Funny!



Solution 5

- We can simulate this with $C1=CL=1\text{pF}$, $G=1\mu\text{S}$ \rightarrow $R=500\text{k}$ yielding corners of 1MHz .



- This can also be seen in a transient sim. with a sine wave:

